

SUMMATIVE ASSESSMENT - III - 2016-2017
MATHEMATICS - PAPER - II
(English Medium)
PRINCIPLE OF VALUATION

Class : IX

SECTION - I

1. Given the interior angles of a triangle = $(3x - 10)^\circ, (3x + 10)^\circ, (3x)^\circ$

$$\text{Sum of the angles} = (3x - 10) + (3x + 10) + 3x = 180^\circ$$

$$9x = 180^\circ$$

$$x = \frac{180^\circ}{9} = 20^\circ$$

$$\begin{aligned} \therefore \text{The angles are} &= [(3 \times 20) - 10], [(3 \times 20) + 10], (3 \times 20) \\ &= 50^\circ, 70^\circ, 60^\circ \end{aligned}$$

2. i) Points that lies on \overline{OY} is for $x = 0, y \geq 0$

The point which satisfies the condition is allowed.

- ii) Points that lies on \overline{OX}^1 is (x, y) for $x = 0, y \leq 0$

The point which satisfies the condition is allowed.

3. Vertically opposite angles

$$\angle AOB = \angle COD \text{ (vertically opposite)}$$

$$\angle AOD = \angle BOC \text{ (vertically opposite)}$$

4. In the $\triangle OAB$

OA = OB = Radius of the circle. In an Isosceles the angles which are opposite to the equal sides are equal.

$$\text{Hence} = \angle OAB = \angle OBA$$

SECTION - II

5. Given data = 10, 15, 20, 25, 15 x
 Arranging in order = 10, 15, 15 x, 20, 25

If mode is x than $x = 15$

Here median is also = 15. $\therefore x = 15$

Sum of scoles = $10 + 3(15) + 20 + 25 = 100$

$$\text{Mean} = \bar{x} = \frac{\sum xi}{n} = \frac{100}{6} = 16\frac{2}{3}$$

6. Given $\overline{EA} \perp \overline{AB}$
 $\overline{DE} \perp \overline{BE}$
 $\overline{CD} \perp \overline{BD}$

Area of ABCDE = Area of $\triangle ABE$

+ Area of $\triangle BED$

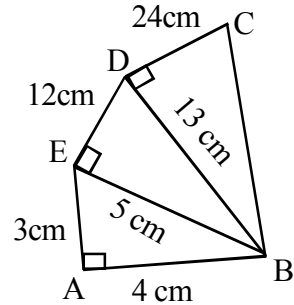
+ Area of $\triangle BDC$

$$\text{Area of } \Delta = \frac{1}{2} \times \text{base} \times \text{high}$$

$$= \frac{1}{2} AB \times AE + \frac{1}{2} BE \times DE + \frac{1}{2} BD \times CD$$

$$= \frac{1}{2} = 4 \times 3 + \frac{1}{2} 5 \times 12 + \frac{1}{2} \times 13 \times 24$$

$$= 6\text{cm}^2 + 30\text{cm}^2 + 156\text{cm}^2 = 192 \text{ cm}^2$$



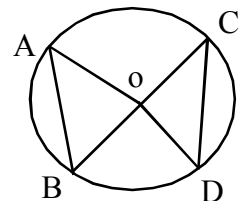
7. Statement : Equal chords of a circle subtend equal angles at the center.

Given : O is the center of a circle

in which $\overline{AB}, \overline{CD}$ two

equal chords. $\angle AOB, \angle COD$

are the angles subtended at the center.



R.T.P. : $\angle AOB = \angle COD$

8. For picking a number (Natural Number) Randomly

Upto $10r$, the possible out comes = 100

$$\text{Probability of an event } P(E) = \frac{\text{No. of required out comes}}{\text{Total out comes}}$$

$$P(E) = \frac{4}{100} = \frac{1}{25}$$

9. Given

Weights in Kg (n)	30	35	40	45
No. of students (f)	10	14	10	6

$$f \cdot x \quad 300 \quad 490 \quad 400 \quad 270$$

$$\text{Mean} = \frac{\sum f \cdot n}{\sum f} = \frac{1460}{40} = 36.5 \text{ kg}$$

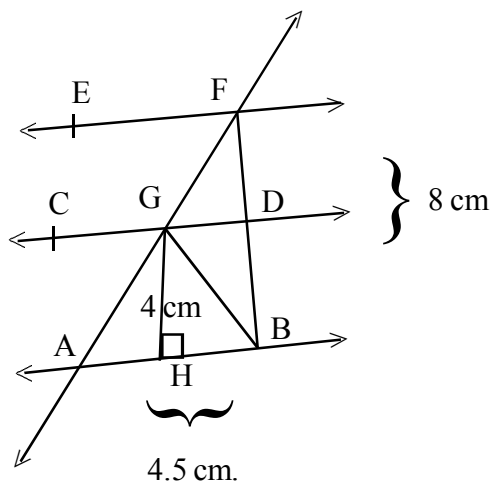
10. a) Given

$\overline{AB} \parallel \overline{CD} \parallel \overline{EF}$
 an equi distance \overline{AF}
 is a transversal

$$\overline{GH} \perp \overline{AB}$$

$$GH = 4 \text{ cm} \quad AB = 4.5 \text{ cm} \quad FB = 8 \text{ cm}$$

To find Area of $\triangle GDF$



In the given figure In $\triangle ABF$ D is the mid point of

\overline{BF} . (Because all the parallel lines are at an equi distance)

Similarly G is the mid point of \overline{AF} (Since $BD = DF$ $AG = GF$)

Hence G is the mid - point. \overline{BD} is the median.

Median divides the triangle into two equal areas.

$$\therefore ar \triangle ABG = ar \triangle BGF$$

Similarly for $\triangle BGF$ \overline{GD} is the median.

$$\therefore ar \triangle ABG = 2 ar \triangle DGF$$

$$ar \triangle DFG = \frac{1}{2} ar \triangle ABG$$

$$\text{Area of } \triangle ABG = \frac{1}{2} \text{ base} \times \text{height} = \frac{1}{2} \times 4.5 \times 4^2 = 9 \text{ cm}^2$$

$$\therefore ar \triangle DGE = \frac{1}{2} \times 9 = 4.5 \text{ cm}^2$$

(or)

b) Area of parallelogram

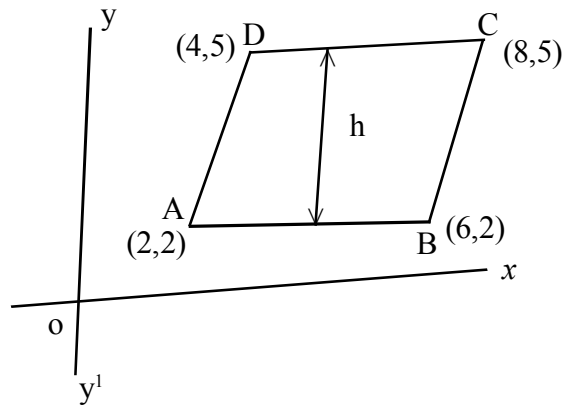
$$= \text{base} \times \text{height}$$

$$= AB \times h$$

$$AB = |x_2 - x_1| = |6 - 2| = 4$$

$$h = |y_2 - y_1| = |5 - 2| = 3$$

$$\text{Area} = 4 \times 3 = 12 \text{ sq. units}$$



11. Given $\overline{AB} \parallel \overline{CD}$

\overline{CE} is a transversal

$\angle DCE, \angle BEC$ are (Interior angles on one side of a transversal)

$$\angle DCE + \angle BEC = 180^\circ \quad \therefore \overline{AB} \parallel \overline{CD}$$

$$\therefore (x + 2y)^\circ = x^\circ = 180^\circ$$

$$2(x + y)^\circ = 180^\circ$$

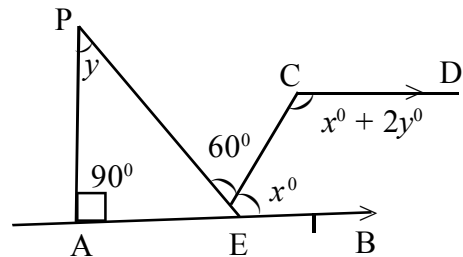
$$(x + y)^\circ = 90^\circ \quad (1)$$

$\angle AEP + \angle PEC + \angle CEB + 180^\circ$ (Angles on one side of a line)

$$\angle AEP + 60^\circ + x^\circ = 180^\circ$$

$$\angle AEP + x^\circ = 120^\circ \quad (2)$$

Now in $\triangle APE$ $\angle APE + \angle PAE + \angle AEP = 180^\circ$



$$y^0 + 90^0 + \underline{AEP} = 180^0 \Rightarrow \underline{AEP} = 90^0 - y^0$$

$$\underline{AEP} + y^0 = 90^0 \quad \text{But from (1)}$$

$$\underline{AEP} + y^0 = x^0 + y^0$$

$$\therefore \underline{AEP} = x^0$$

$$\text{Substiting in (2) } x^0 + x^0 = 120^0 \Rightarrow x = 60^0$$

$$\therefore y^0 = 90^0 - x^0 = 90^0 - 60^0 = 30^0$$

(or)

b)

Weight (kg) (x)	No. of Parcel (f)	f × x	c.f.
50	25	1250	25
65	34	2210	59
75	38	2850	97
90	x	90x	97+x
110	47	5170	144+x
120	16	1920	160+x

Median class

$$(160+x) \quad 13,400 + 90x$$

$$\text{Mean} = 85 \text{ (Given)}$$

$$\text{Mean} = \frac{\sum f.x}{\sum f} = \frac{13,400 + 90x}{160 + x} = 85$$

$$= 13,400 + 90x = 13600 + 85x$$

$$90x - 85x = 13,600 - 13,400 = 200$$

$$5x = 200$$

$$x = 40$$

$$\text{Median} : \therefore N \text{ is } 160 + 40 = 200 \text{ even}$$

$$\text{Median} = \left(\frac{N}{2} + 1 \right)^{\text{th}} = 101^{\text{th}}$$

$$101^{\text{th}} \text{ frequency is } = 90$$

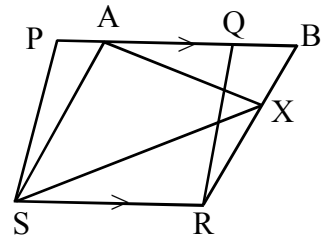
$$\text{Median} = 90$$

12. a) In the given figure
' PQRS and ' ABRS
are two parallelogram on the same
base \overline{SR} .

$$\text{Hence ar ' PQRS} = \text{ar ' ABRS} \quad - (1)$$

In ' ABRS ΔASX is the triangle on the same base \overline{AS}

$$\text{Hence ar } \Delta ASX = \frac{1}{2} \text{ ar ' PQRS}$$



(or)

b) In the given figure

$\overline{CD} \perp \overline{AB}$ (perpendicular bisector)

Given O is the centre of the circle.

$\overline{AB} \perp \overline{CD}$

To prove: $\overline{AD} = \overline{BD}$

Construction: Join $\overline{AD}, \overline{BD}$

Proof: In $\triangle AED, \triangle BE$

$\overline{AE}, \overline{BE}$ (Perpendicularly bisects)

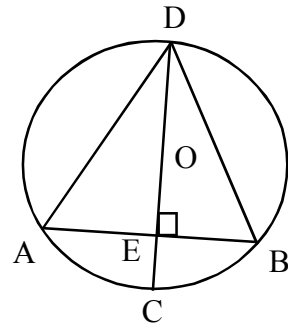
$\overline{DE}, \overline{DE}$ (Common side)

$\angle AED = \angle BED = 90^\circ$

under Rh.S congruency or (S.A.S) congruency

$\triangle AED \cong \triangle BED$

under CPCT $\overline{AD} = \overline{BD}$



13. a) Construction of triangle - 1

Construction of circum circle - 1½

Steps of construction: 1

b) Construction - 2½

Steps of construction

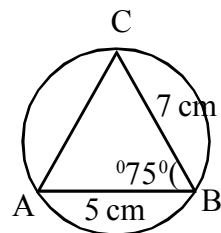
Draws a line segment $\overline{BC} = 5\text{cm}$

Draw an angle $\angle ABC = 60^\circ$

Since $\overline{AB} + \overline{AC} = 8\text{cm}$ take $BD = 8\text{cm}$

Draw an arc from B by taking 8 cm as radius.

Join \overline{CD}



Draw a perpendicular bisect to \overline{CD}

If intersect \overline{BD} at A

Join \overline{AC} our required ΔABC obtained.

PART - B

- | | | | |
|-----|---|-----|---|
| 14. | B | 26. | D |
| 15. | C | 27. | A |
| 16. | A | 28. | B |
| 17. | D | 29. | D |
| 18. | C | 30. | C |
| 19. | A | 31. | D |
| 20. | A | 32. | B |
| 21. | C | 33. | B |
| 22. | C | | |
| 23. | D | | |
| 24. | B | | |
| 25. | C | | |